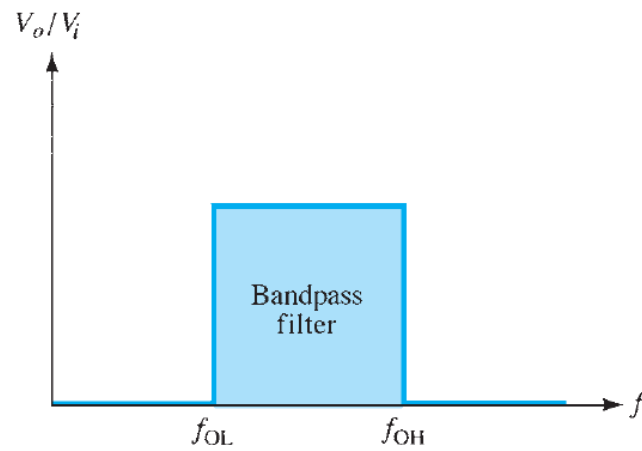
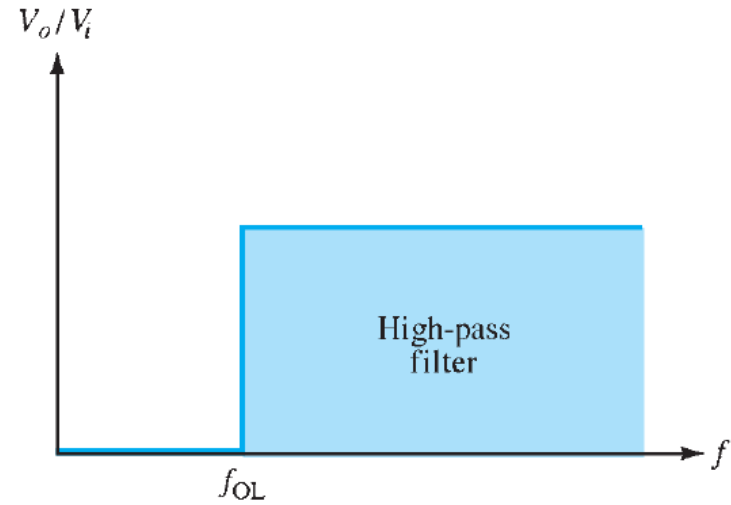
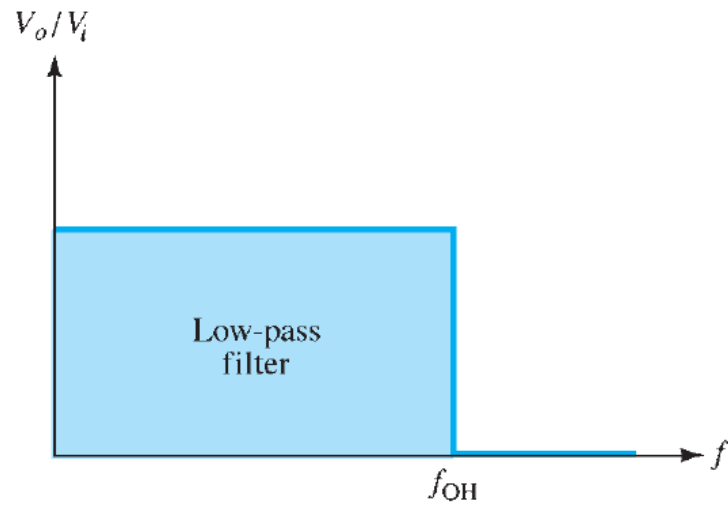
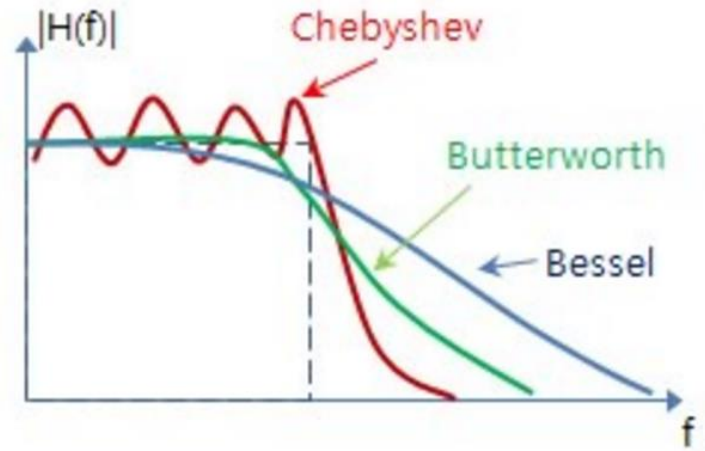
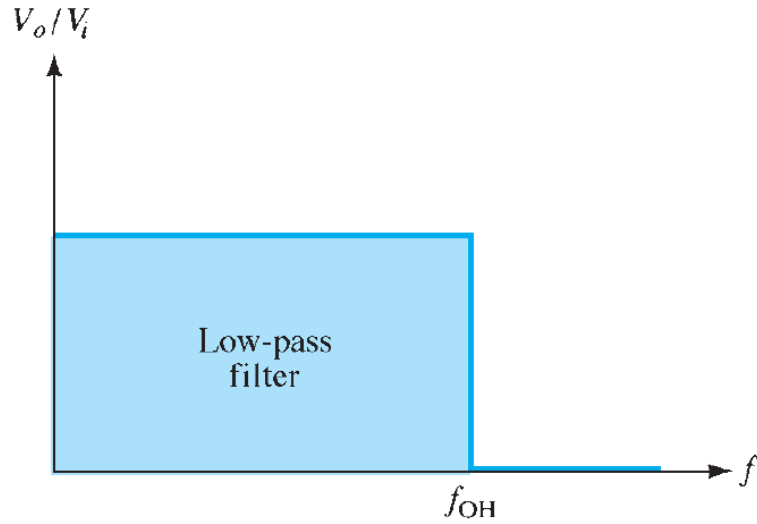


Active Filters

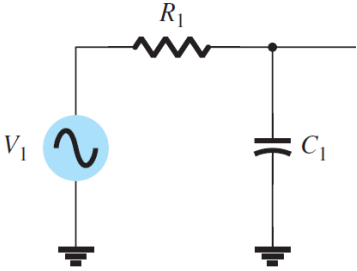
Active Filters



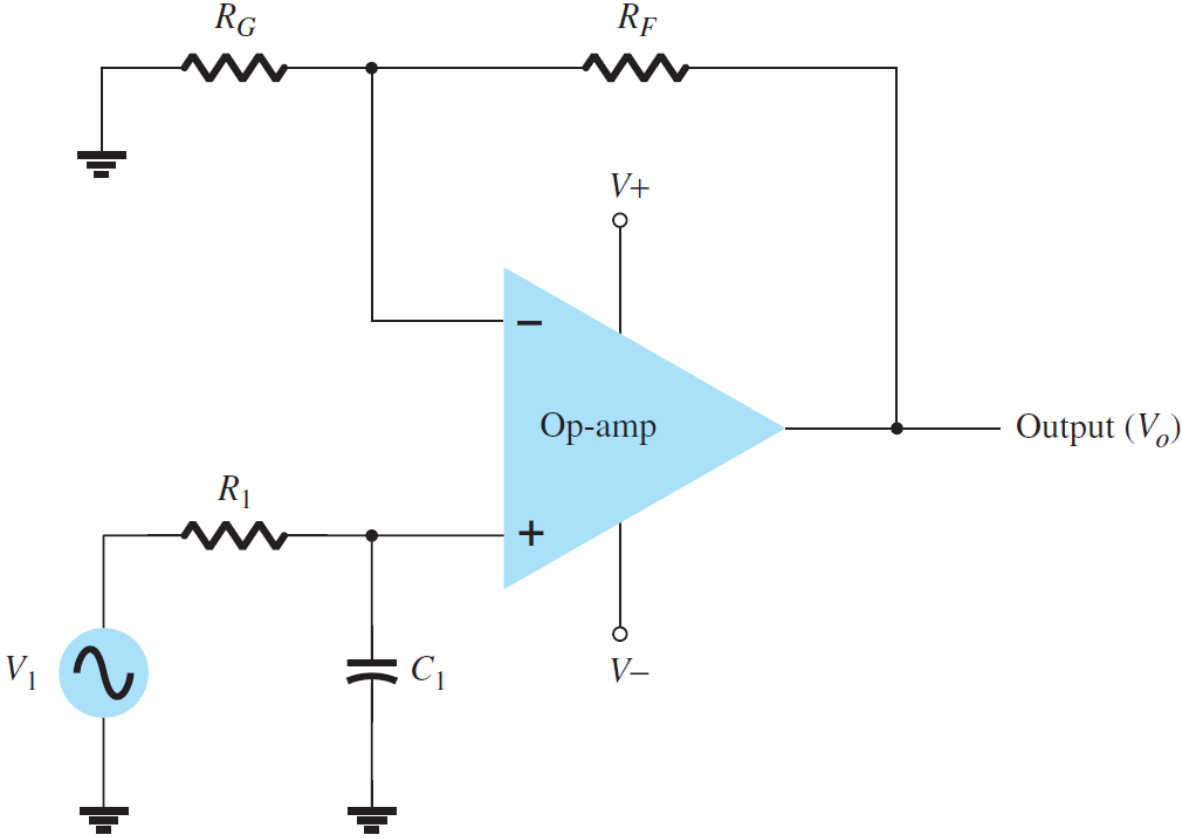
Ideal and Practical Filters



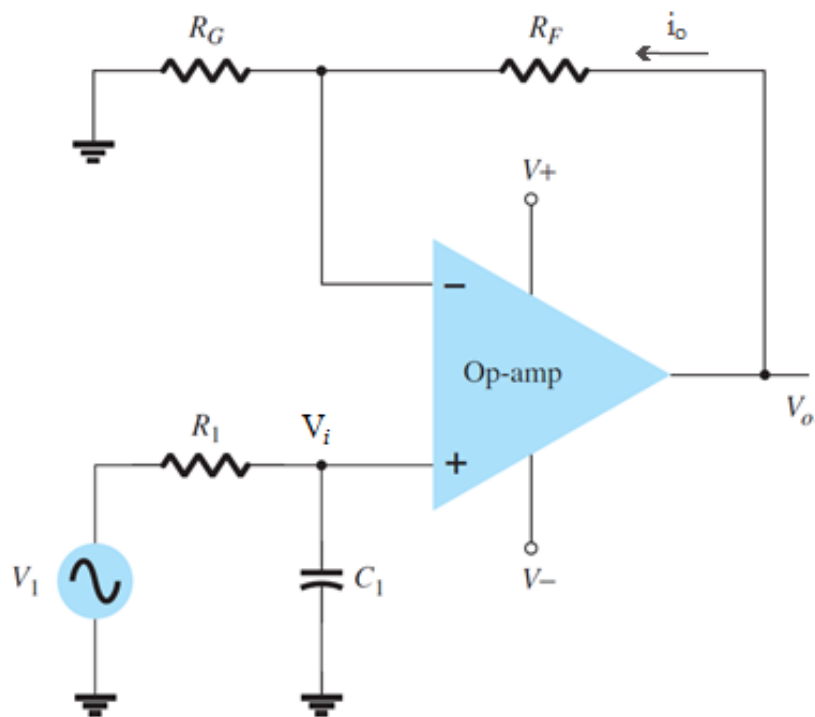
Active Filters



RC Low-pass filter



Active Filters



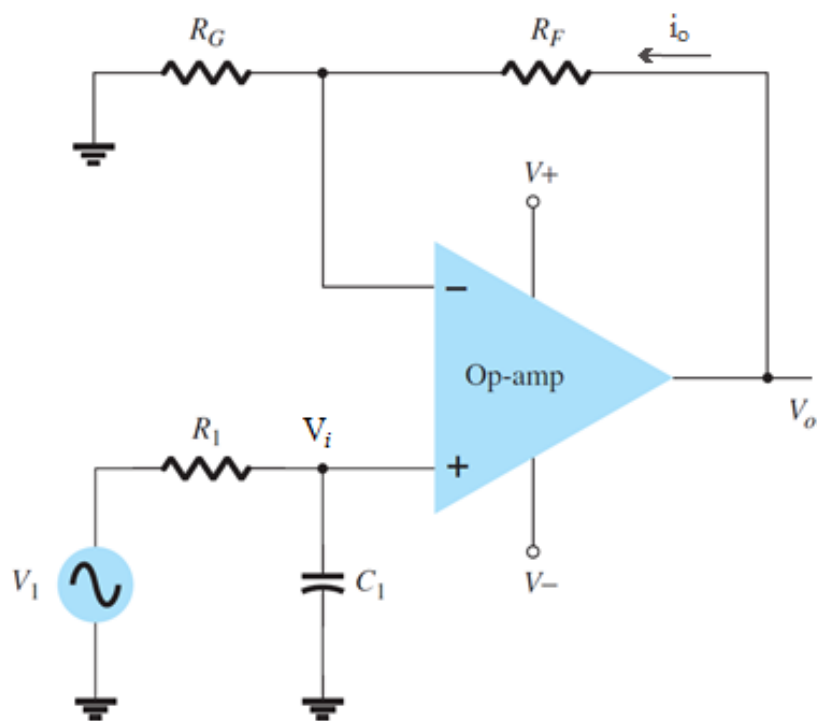
$$V_i = \frac{V_1}{R_1 + \frac{1}{j\omega C_1}} \cdot \frac{1}{j\omega C_1} \Rightarrow V_i = \frac{V_1}{1 + j\omega R_1 C_1}$$

$$i_o = \frac{V_o - V_i}{R_F} \approx \frac{V_i}{R_G} \Rightarrow V_o = \left(1 + \frac{R_F}{R_G}\right) V_i$$

Combining:

$$V_o = \left(1 + \frac{R_F}{R_G}\right) \left(\frac{1}{1 + j\omega R_1 C_1}\right) V_1$$

Active Filters



$$\frac{V_o}{V_1} = A_v = \left(1 + \frac{R_F}{R_G} \right) \left(\frac{1}{1 + j\omega R_1 C_1} \right)$$

Real
number
(gain)

Low-pass
filter

>1 for a
low-pass
filter
with
voltage
gain

$$f_{oL} = \frac{1}{2\pi R_1 C_1}$$

cut-off
frequency

Active Filters

$$\frac{V_o}{V_1} = A_v = \left(1 + \frac{R_F}{R_G}\right) \left(\frac{1}{1 + j\omega R_1 C_1}\right)$$

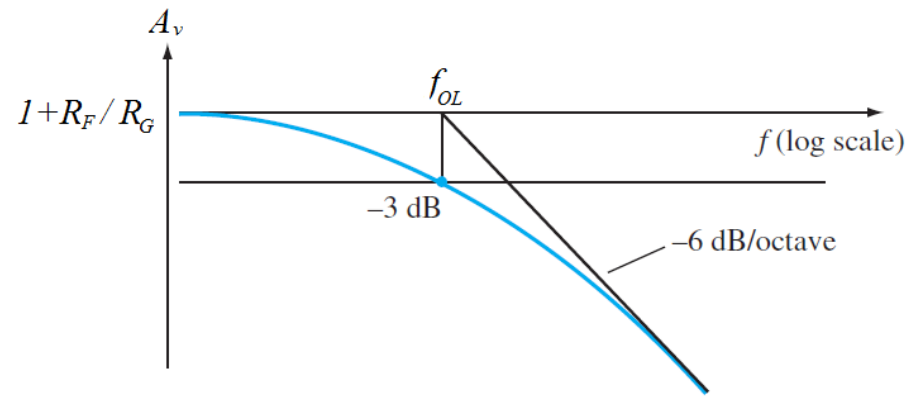
Real
number
(gain)

>1 for a
low-pass
filter
with
voltage
gain

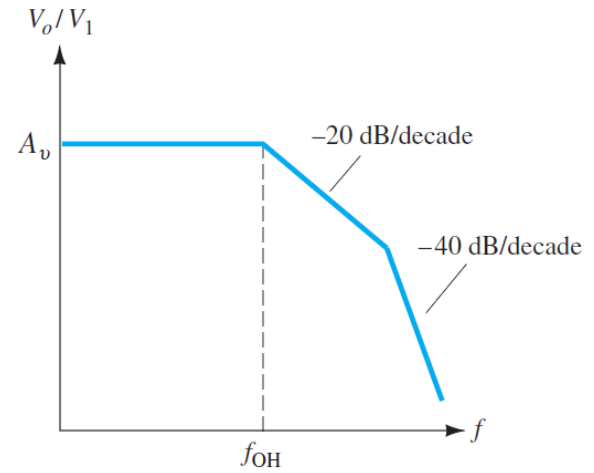
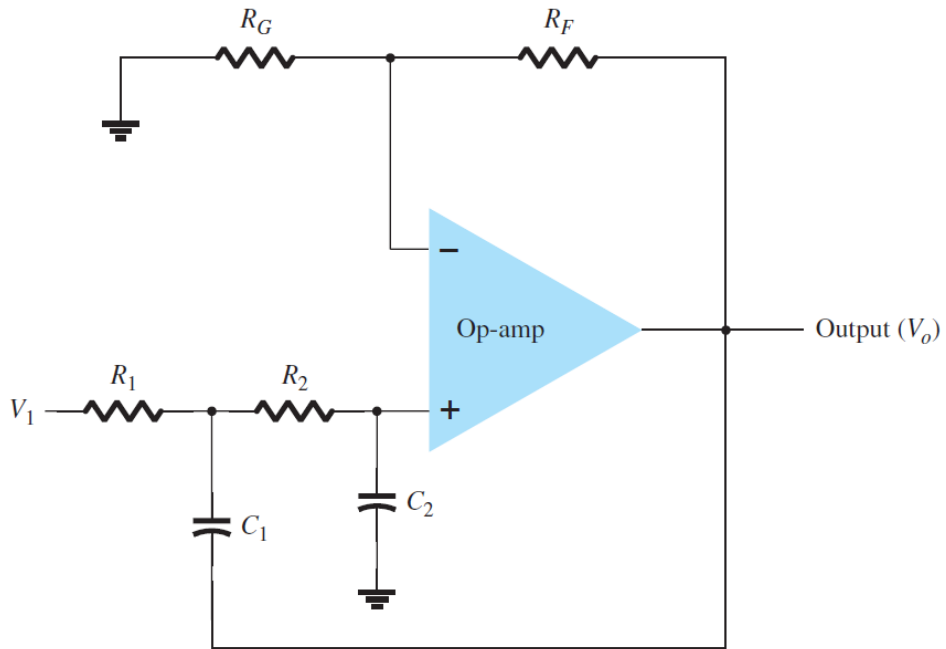
Low-pass
filter

$$f_{OL} = \frac{1}{2\pi R_1 C_1}$$

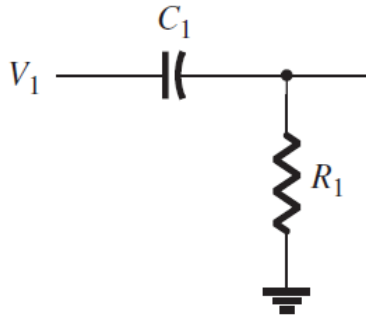
cut-off
frequency



Active Filters



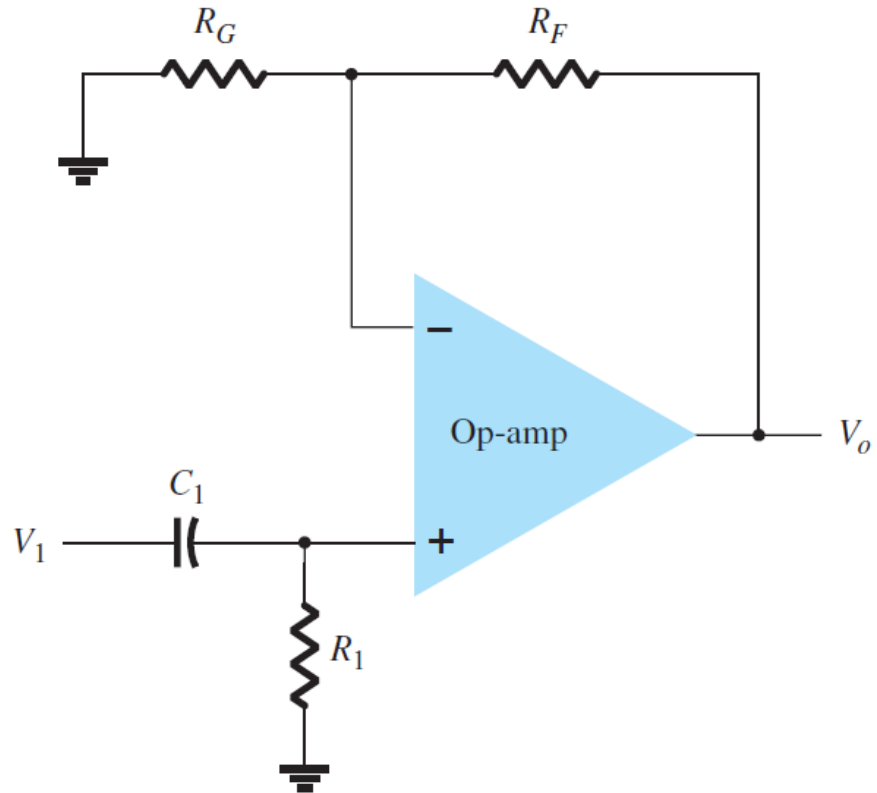
Active Filters



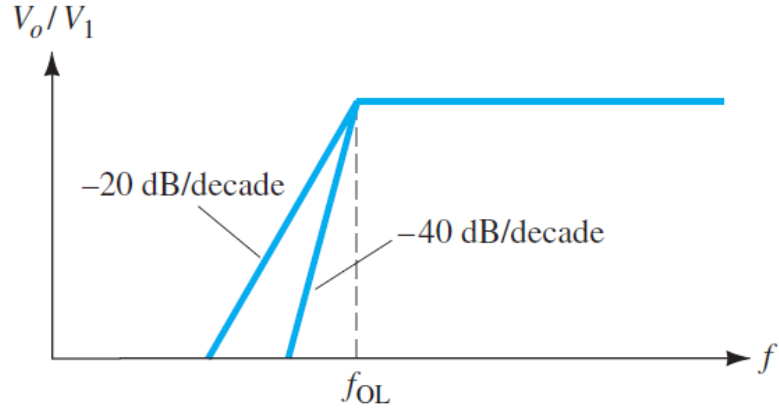
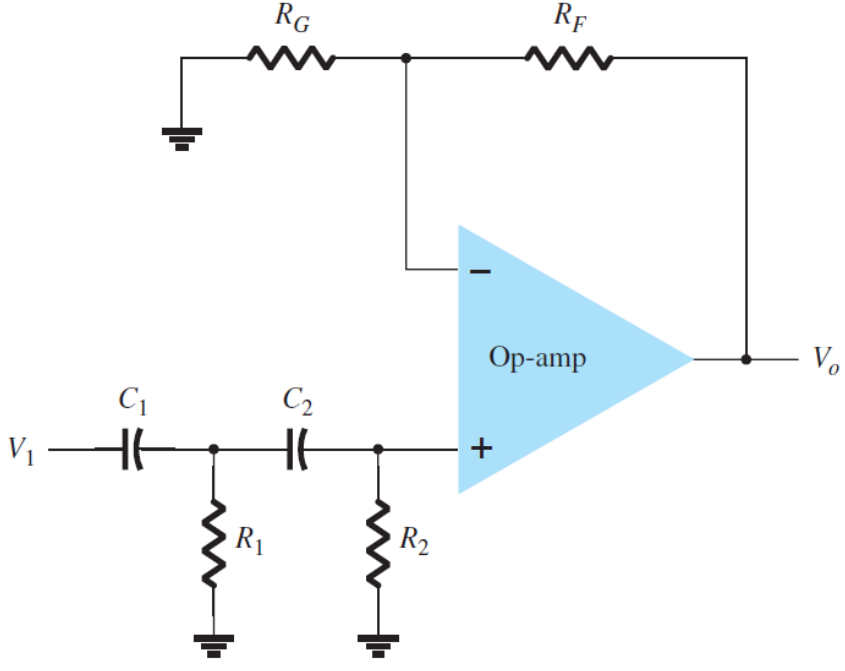
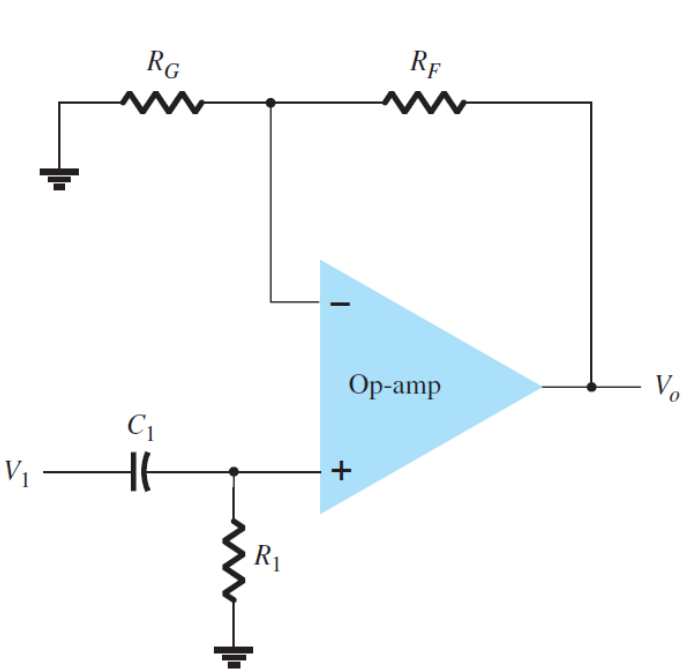
RC High-pass filter

$$A_v = \left(1 + \frac{R_F}{R_G} \right)$$

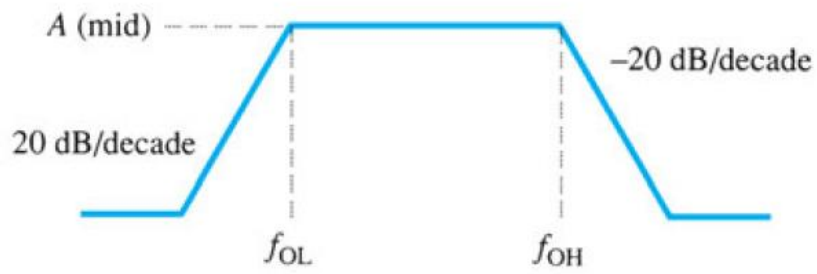
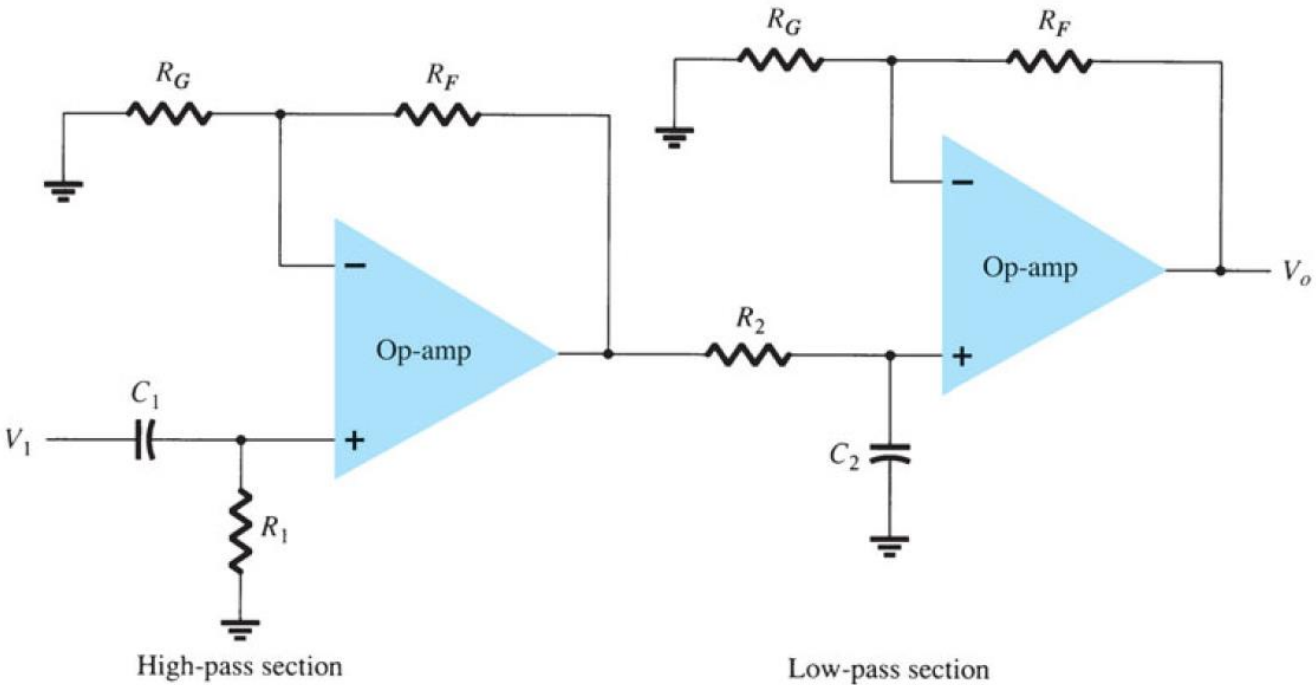
$$f_{OH} = \frac{1}{2 \pi R_1 C_1}$$



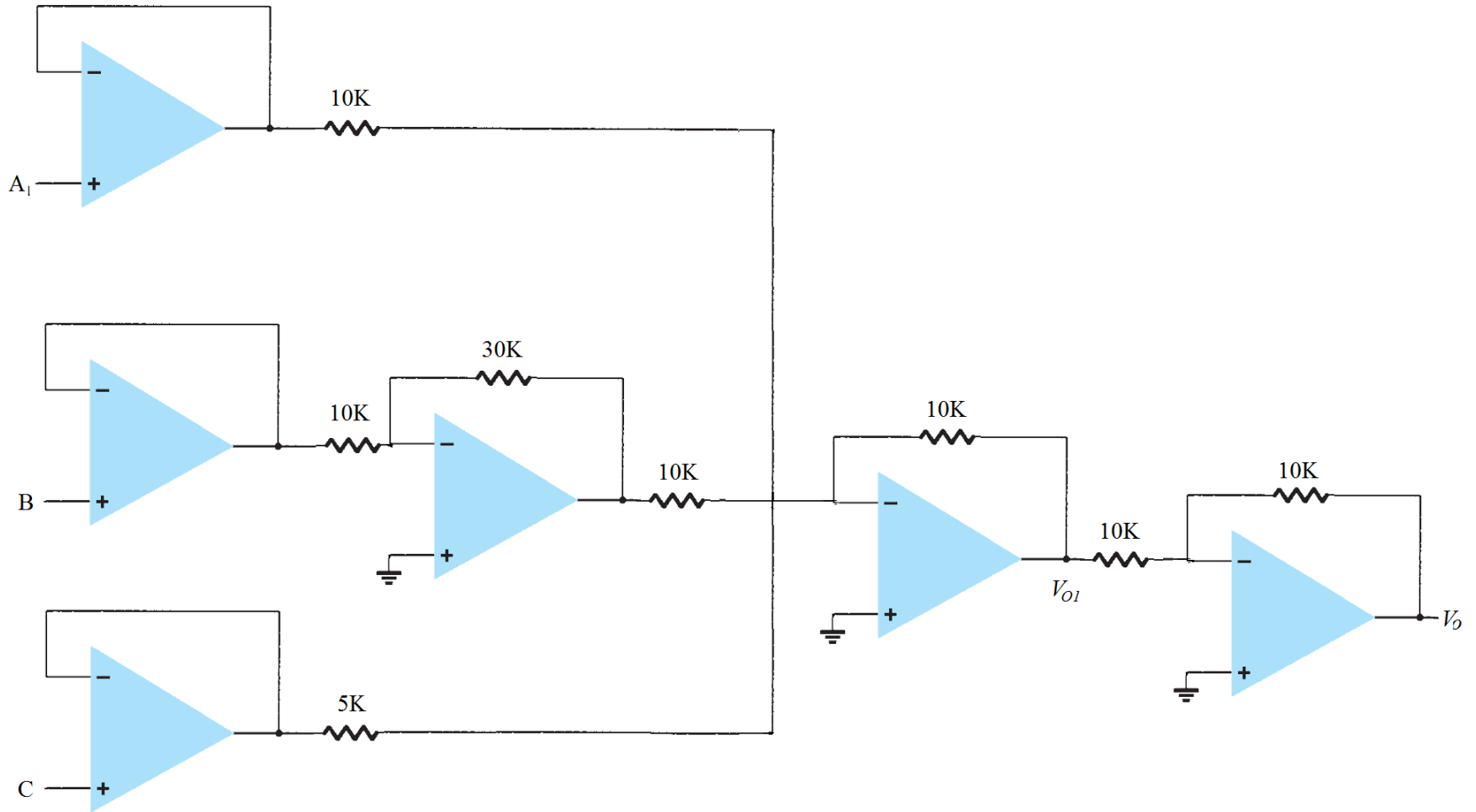
Active Filters



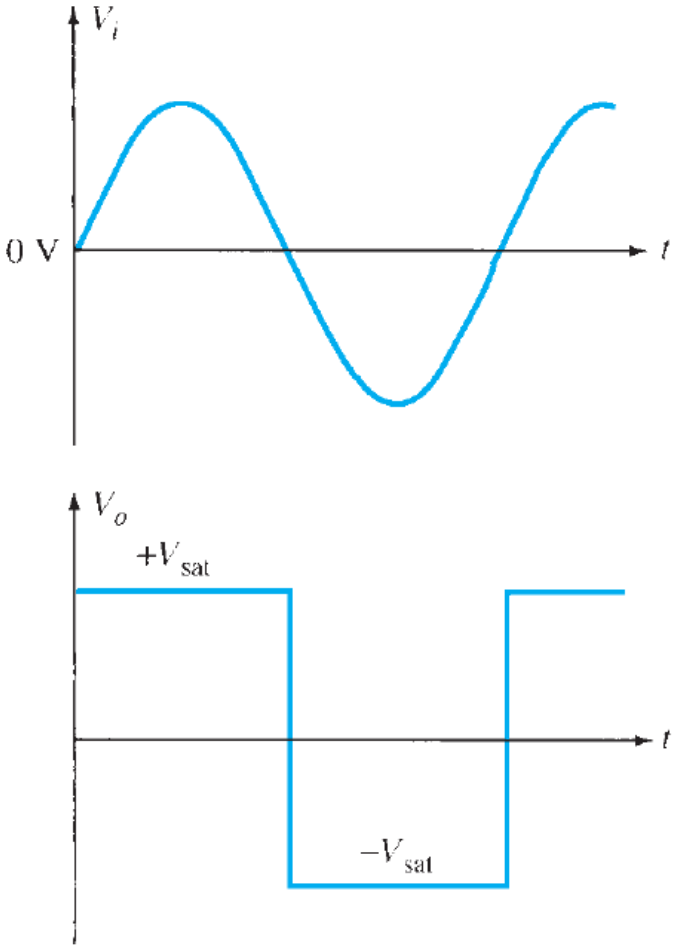
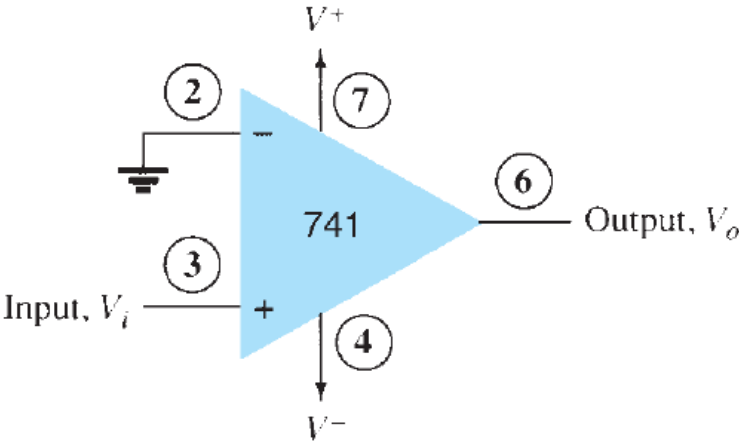
Active Filters



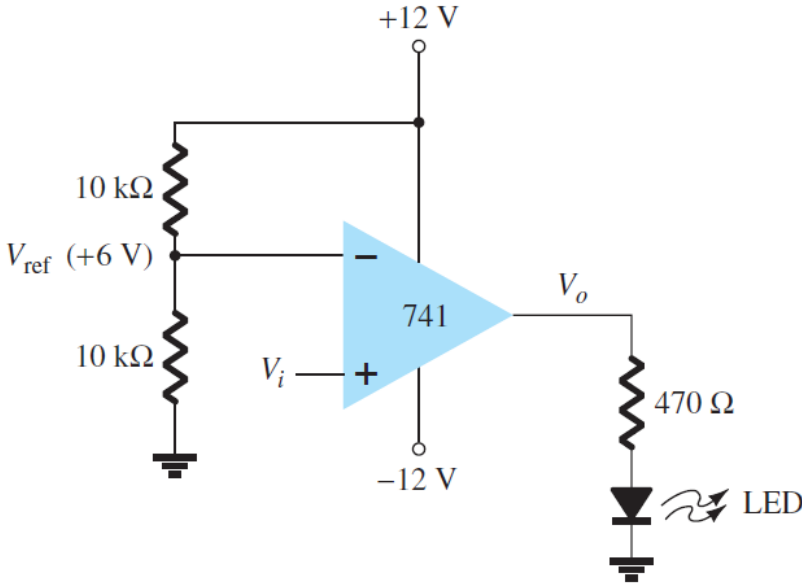
Example Applications



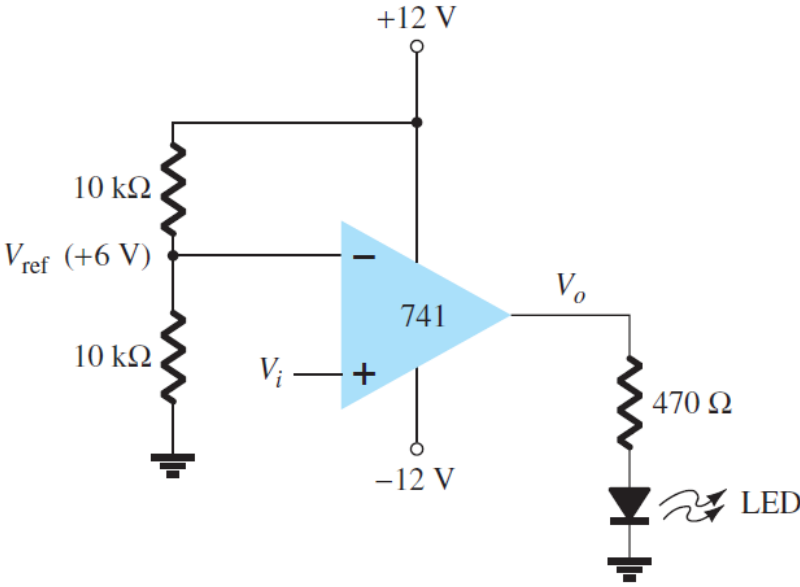
Linear Integrated Circuits



Linear Integrated Circuits

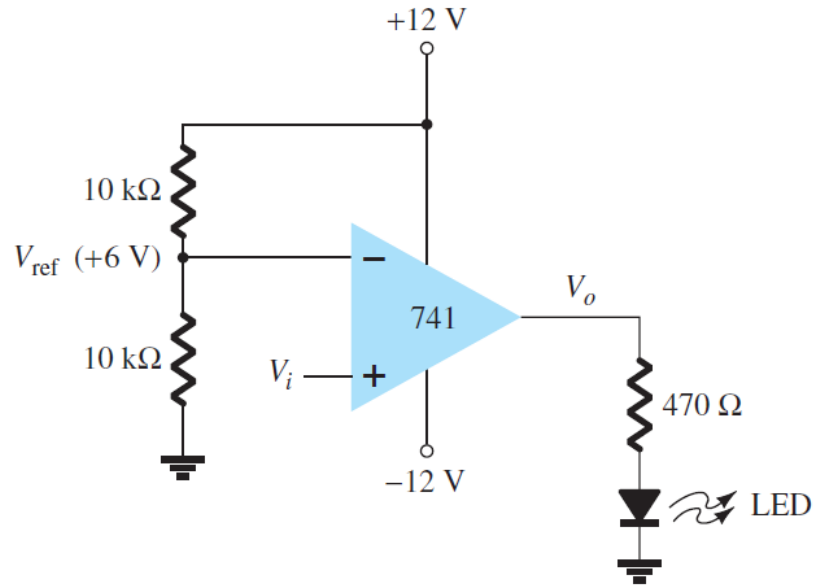


Linear Integrated Circuits

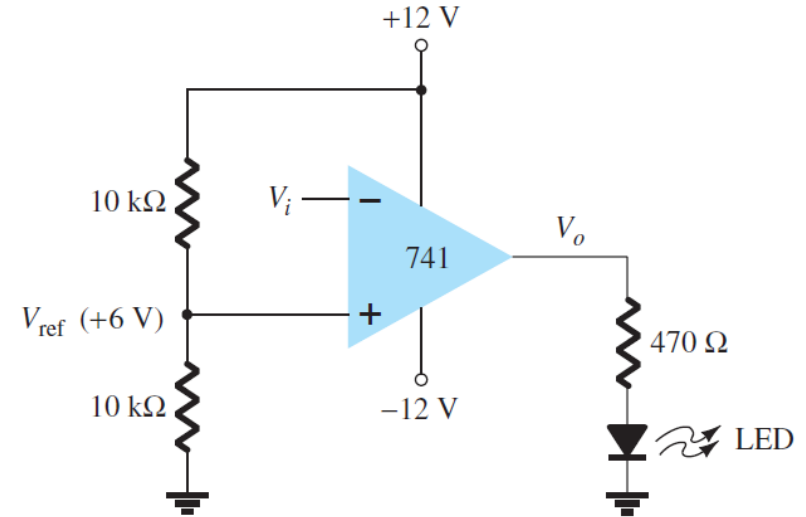


LED *on* when
 V_i goes above
 V_{ref} (= +6 V)

Linear Integrated Circuits

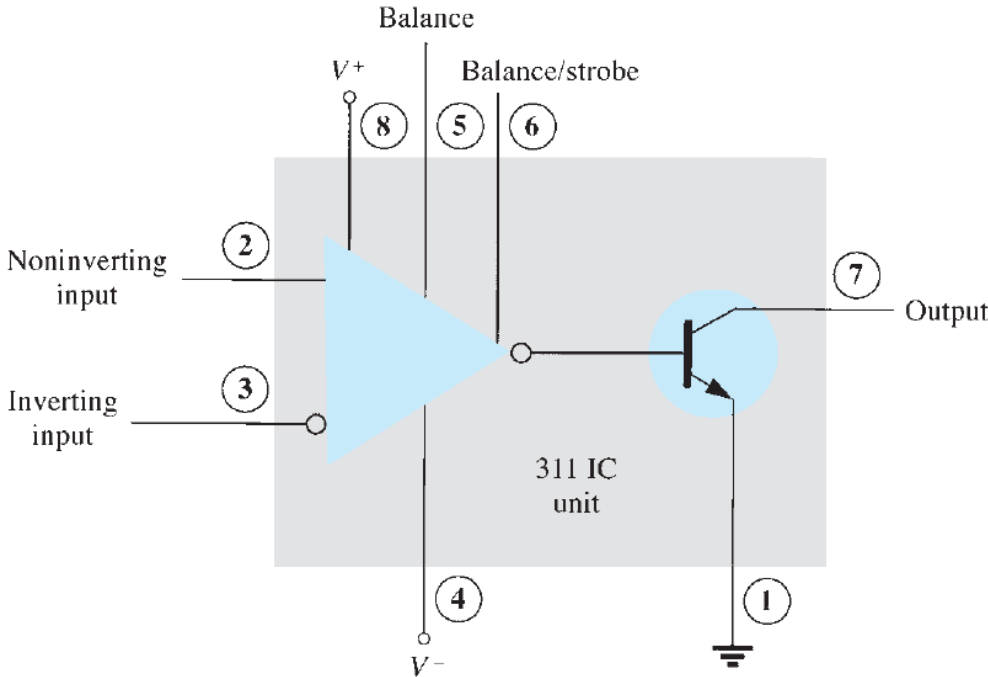


LED on when
 V_i goes above
 $V_{\text{ref}} (= +6 \text{ V})$

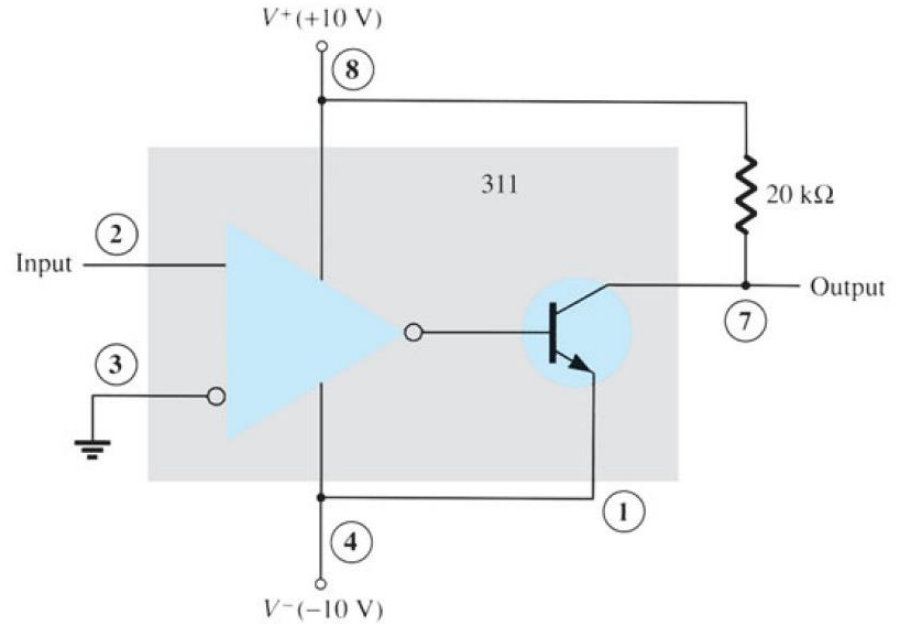
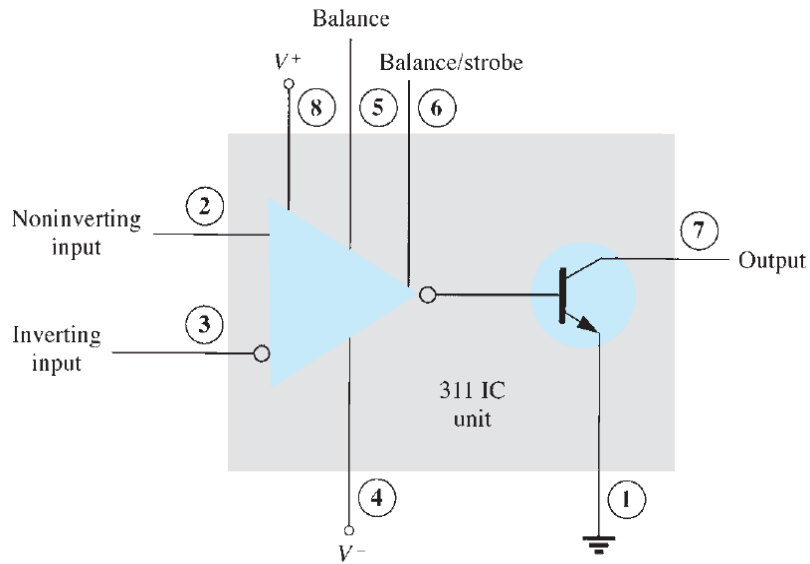


LED on when
 V_i goes below
 $V_{\text{ref}} (= +6 \text{ V})$

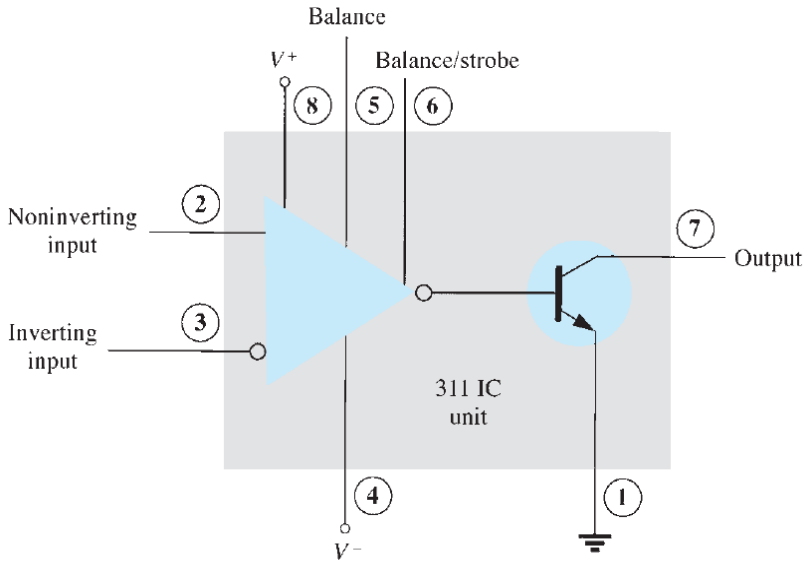
Linear Integrated Circuits – IC 311 Comparator



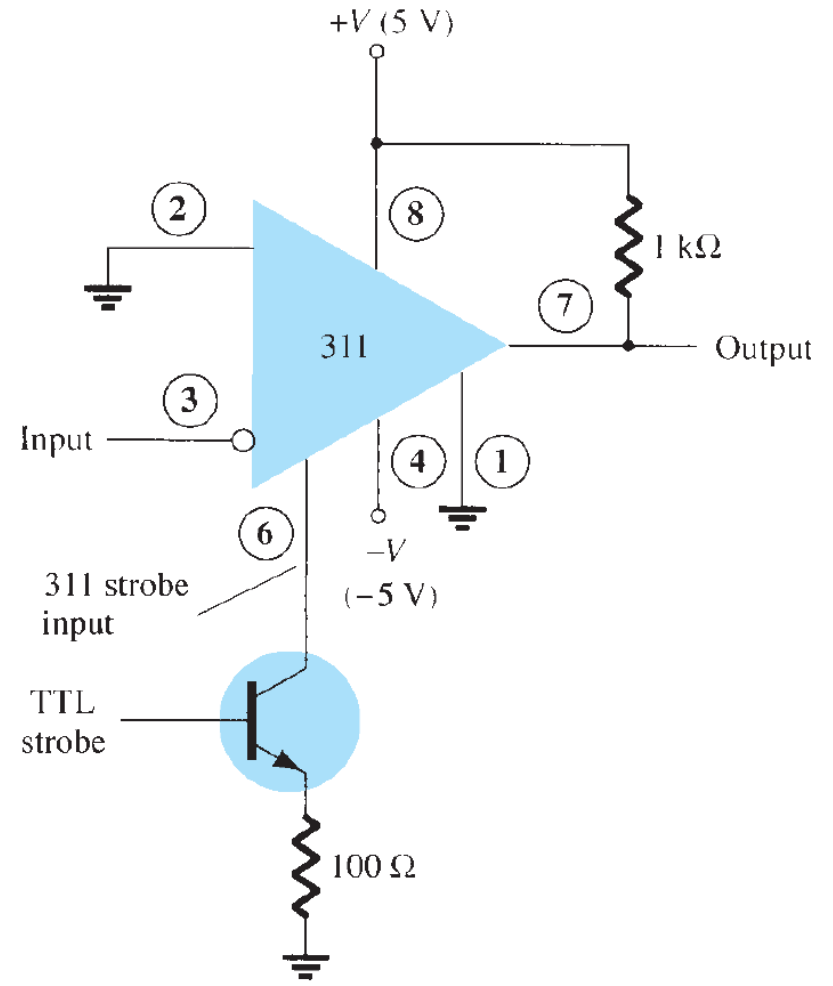
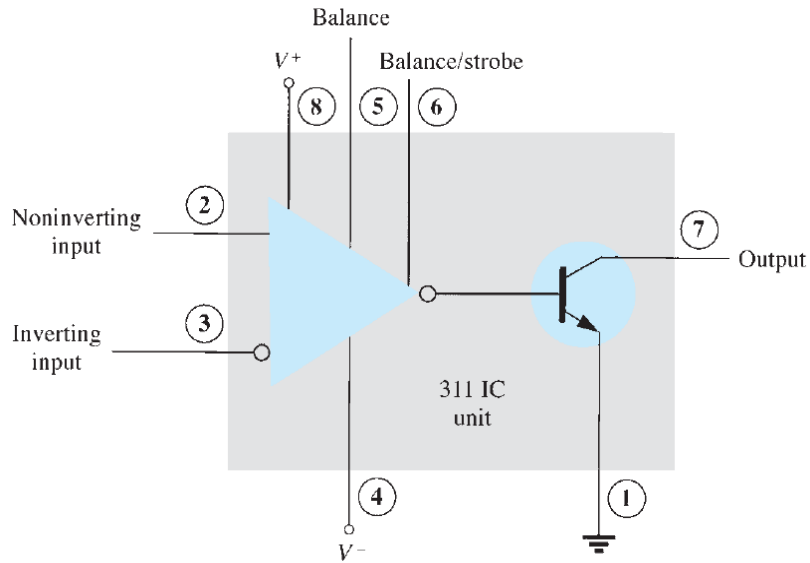
Linear Integrated Circuits – IC 311 Comparator



Linear Integrated Circuits – IC 311 Comparator



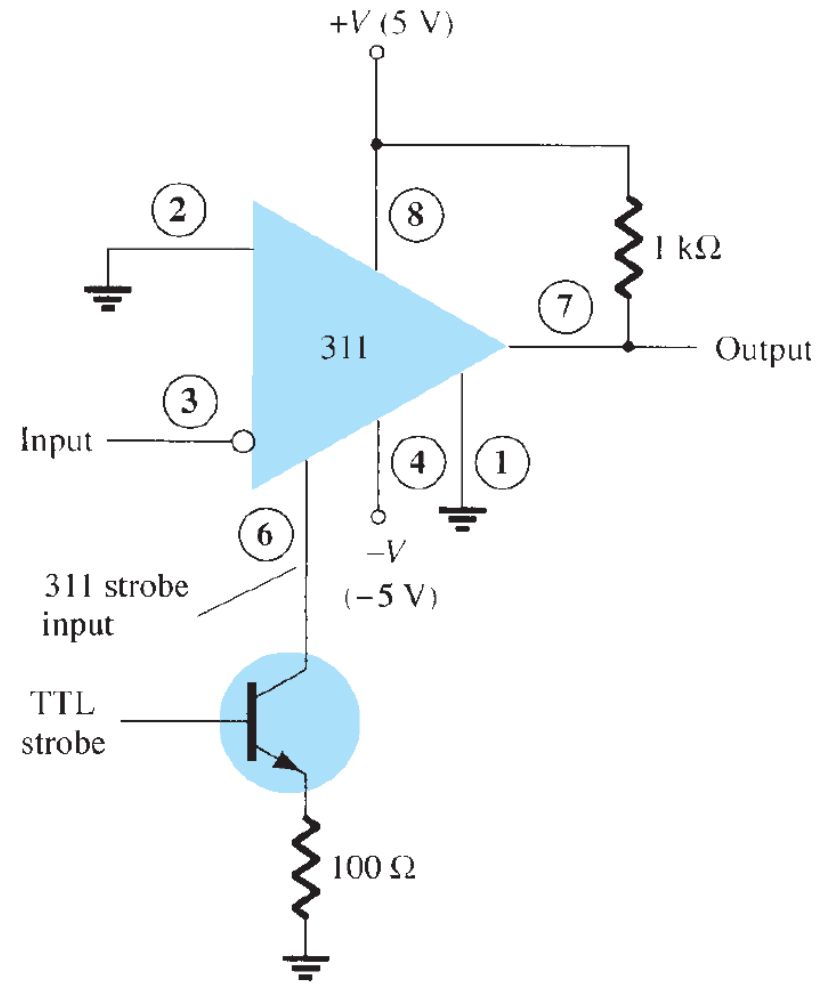
Linear Integrated Circuits – IC 311 Comparator



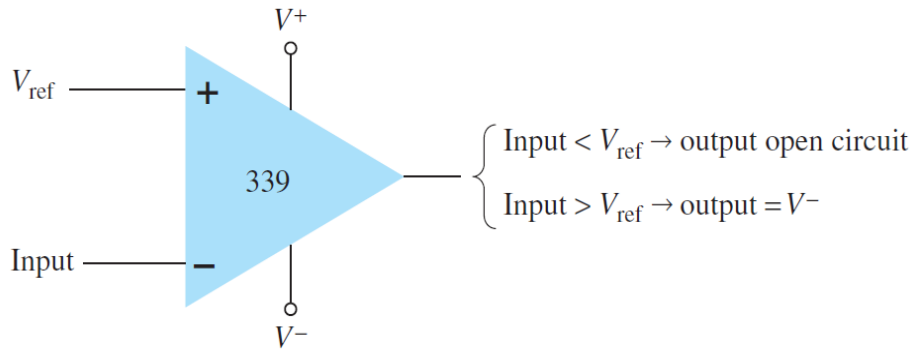
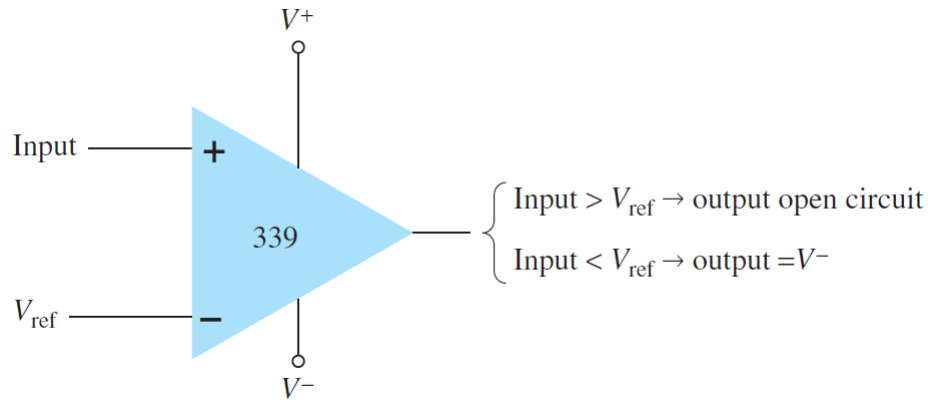
Linear Integrated Circuits – IC 311 Comparator

If $V_{in} > 0\text{ V}$ (V_{ref}), V_o is HIGH if TTL Strobe is OFF

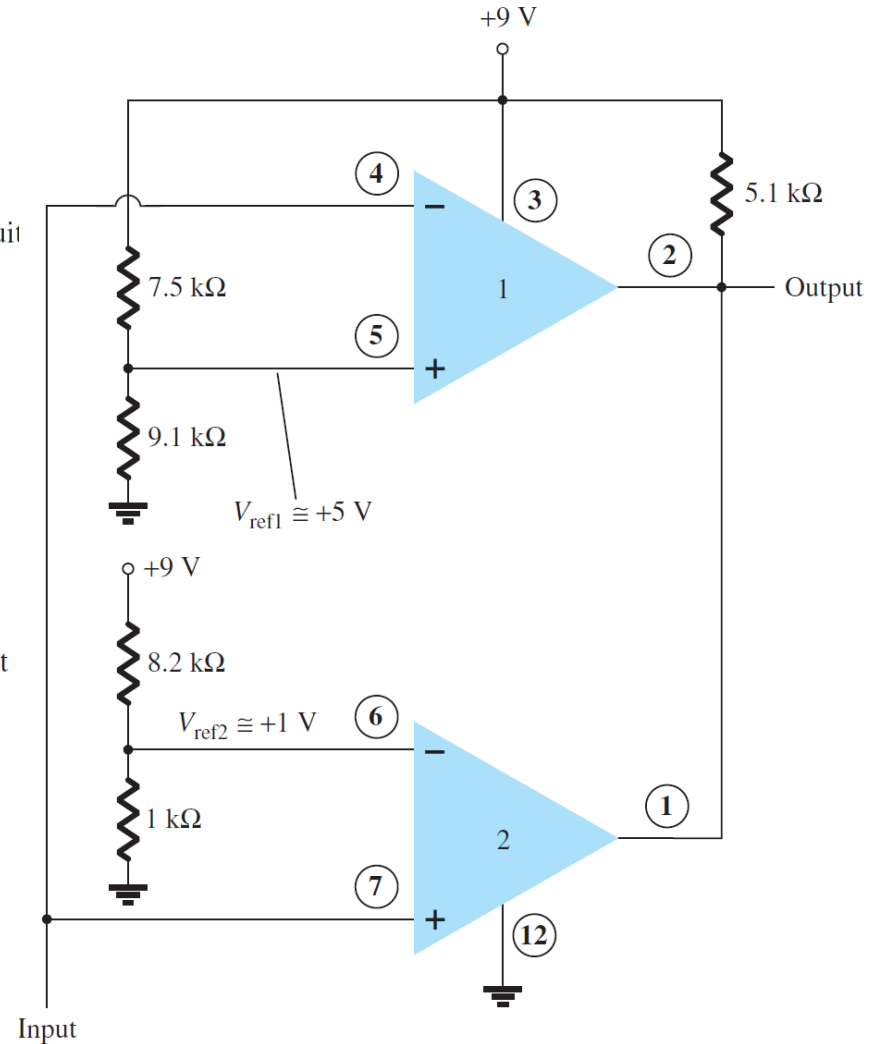
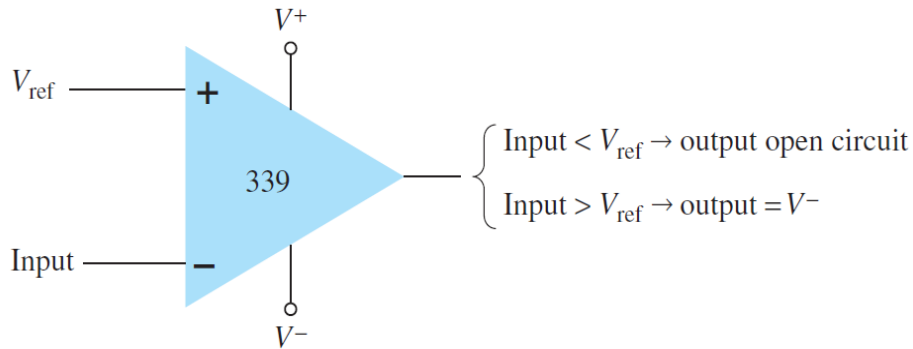
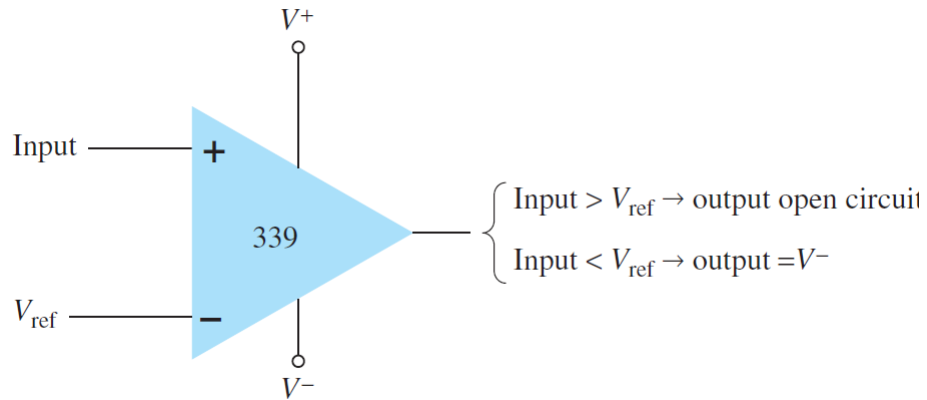
If TTL Strobe goes HIGH, $V_o = \text{HIGH}$ regardless of input



Linear Integrated Circuits – IC 339 Comparator

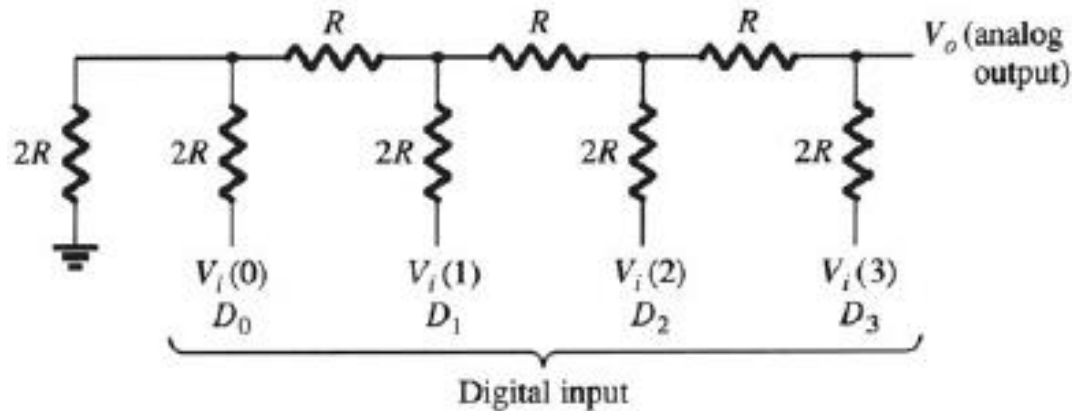


Linear Integrated Circuits – IC 339 Comparator



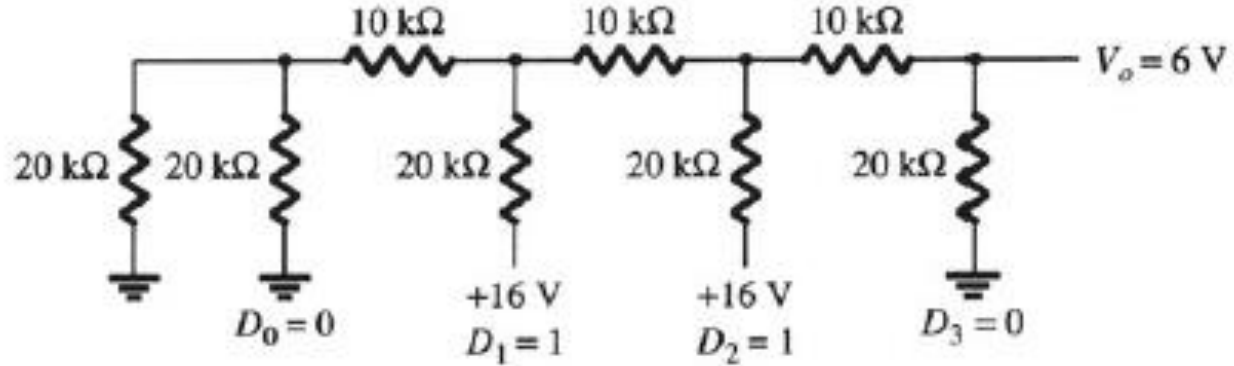
Linear Integrated Circuits – Digital to Analog Converters (DAC)

Ladder Network Conversion



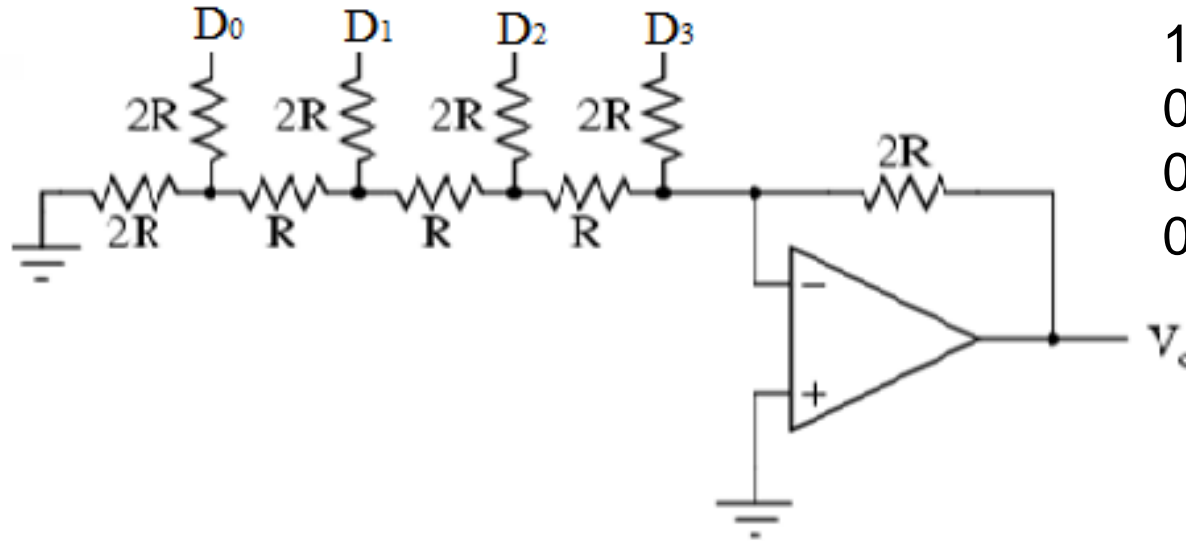
$$V_o = \frac{D_0 \times 2^0 + D_1 \times 2^1 + D_2 \times 2^2 + D_3 \times 2^3}{2^4} V_{\text{ref}}$$

Linear Integrated Circuits – DAC



$$V_o = \frac{0 \times 1 + 1 \times 2 + 1 \times 4 + 0 \times 8}{16} (16 \text{ V}) = 6 \text{ V}$$

Linear Integrated Circuits – DAC



1000 → $V_o = -5V$
 0100 → $V_o = -2.5V$
 0010 → $V_o = -1.25V$
 0001 → $V_o = -0.625V$

0 0000 → $V_o = 0V$
 1 0001 → $V_o = -0.625V$
 2 0010 → $V_o = -1.25V$
 3 0011 → $V_o = -1.875V$

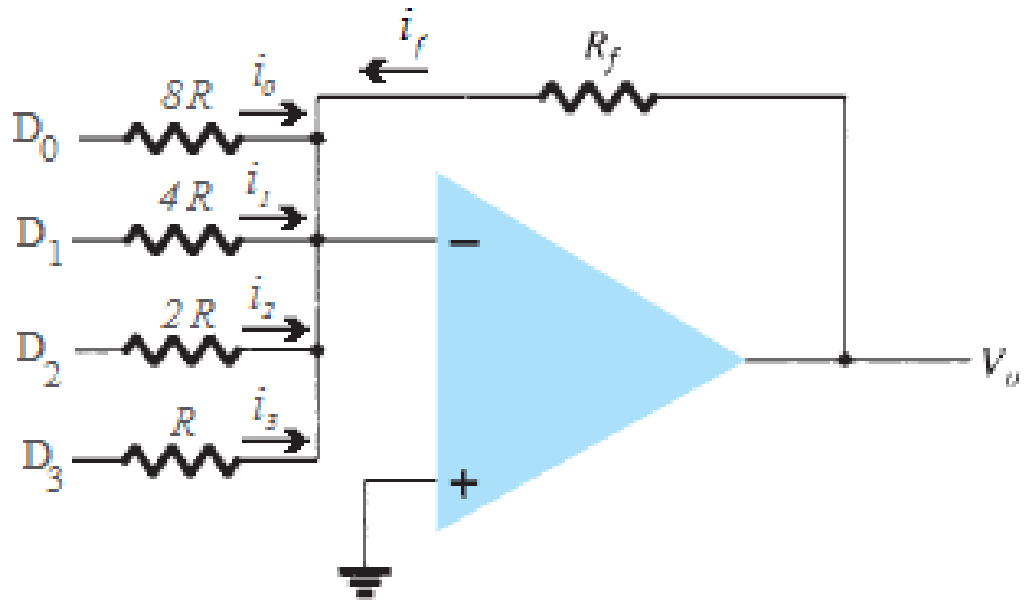
$(0101)_2 = (5)_{10}$
 ⇒ $V_o = -2.5 - 0.625 = -3.125V$

·
·
·

15 1111 → $V_o = -9.375V$

Linear Integrated Circuits – DAC

Binary Weighted DAC



$$i_0 = \frac{V}{8R}$$

$$i_1 = \frac{V}{4R}$$

$$i_2 = \frac{V}{2R}$$

$$i_3 = \frac{V}{R}$$

$$i_f = \frac{V_o}{R_f}$$

$$i_f = -(i_0 + i_1 + i_2 + i_3)$$

$$V_o = -R_f V \left(\frac{1}{8R} + \frac{1}{4R} + \frac{1}{2R} + \frac{1}{R} \right)$$

Linear Integrated Circuits – DAC

Performance Characteristics:

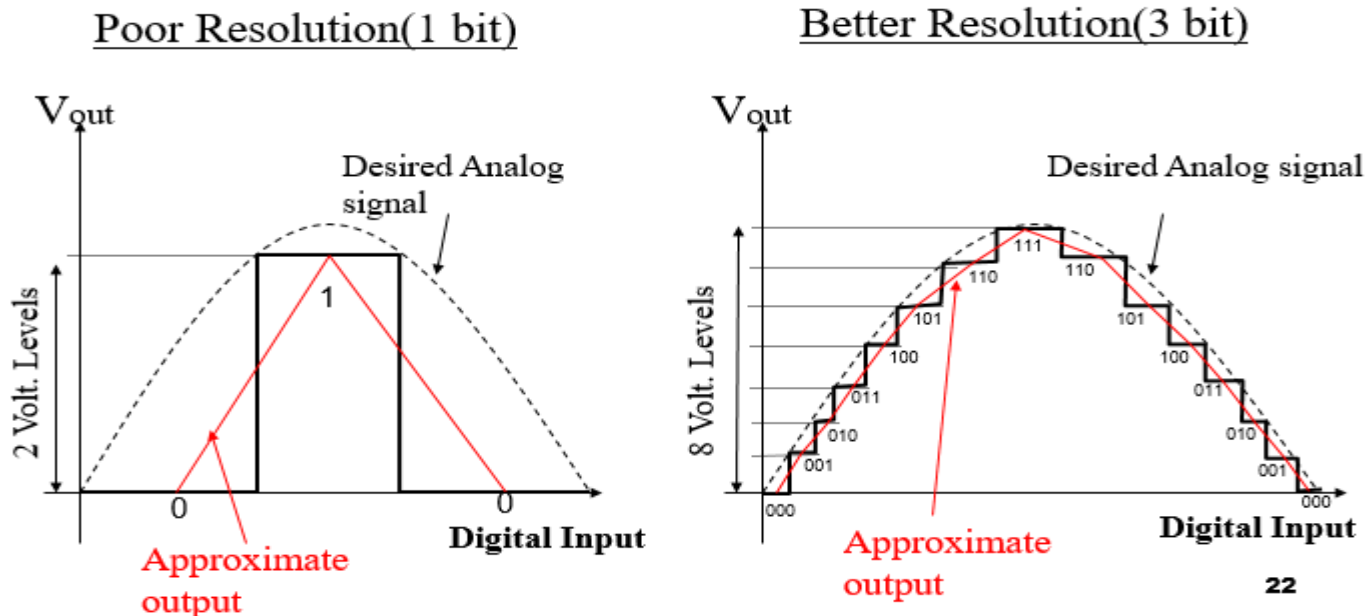
1. Resolution
2. Accuracy
3. Linearity
4. Monotonicity
5. Settling time

Linear Integrated Circuits – DAC

Resolution: Can be defined as

- the of number of bits (i.e., n)
- The number of steps (i.e., $2^n - 1$)

How closely can we approximate the desired output signal (Higher Res. = finer detail = smaller Voltage divisions)



Linear Integrated Circuits – DAC

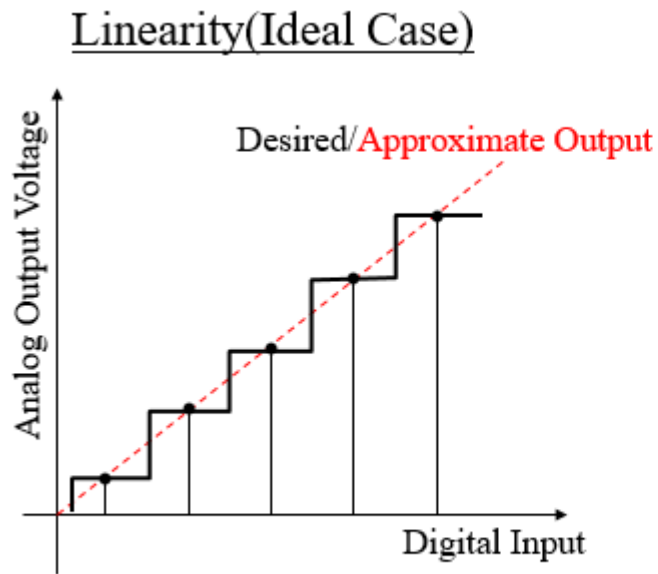
Accuracy: A comparison of the actual output of a DAC with the expected output. At the worst case, accuracy is $V_{\text{ref}}/2^n$

- Expressed as a percentage of a full-scale, or maximum, output voltage
- For example, if a converter has a full-scale output of 10V and the accuracy is $\pm 0.1\%$, then the maximum error for any output voltage is $(10\text{ V})(0.001) = 10\text{ mV}$
- For an 8-bit converter, 1 LSB is $1/256 = 0.0039$ (0.39% of full scale). Accuracy is approximately $\pm 0.2\%$

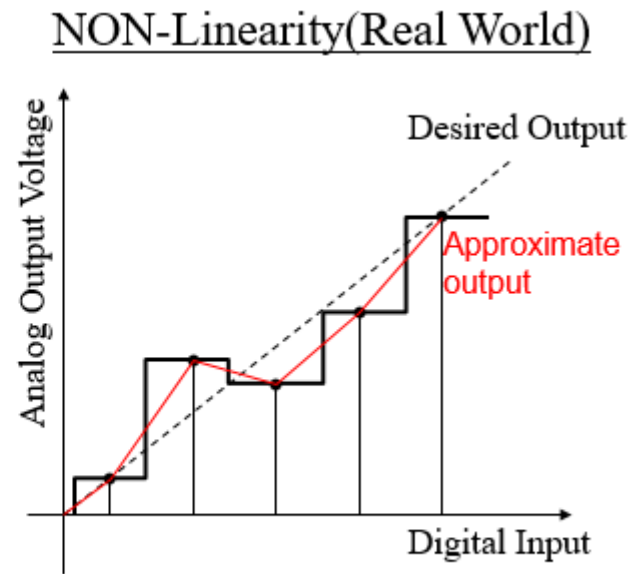
Linear Integrated Circuits – DAC

Linearity: the difference between the desired analog output and the actual output over the full range of expected values.

- Ideally, a DAC should produce a linear relationship between a digital input and the analog output, this is not always the case.
- Any change in the input state will not be reflected in the output state immediately. There is a time lag, between the two events



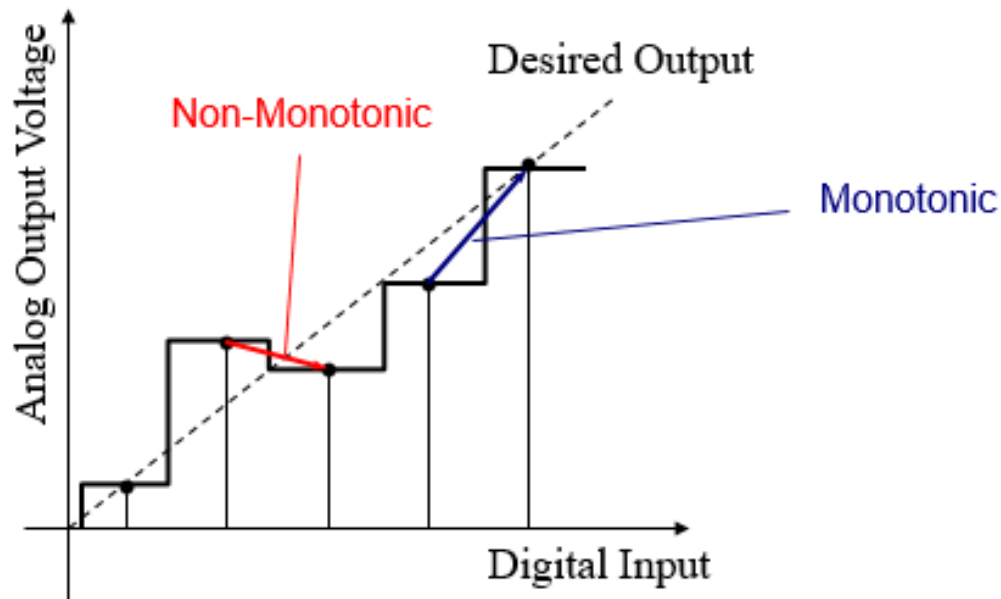
Perfect Agreement



Miss-alignment

Linear Integrated Circuits – DAC

Monotonicity: A DAC is monotonic if it does not take any reverse steps when it is sequenced over its entire range of input bits.



Linear Integrated Circuits – DAC

Settling Time

- The time required for the input signal voltage to settle to the expected output voltage (within $\pm V_{LSB}$).
- Any change in the input state will not be reflected in the output state immediately. There is a time lag, between the two events

